# Stable Control of Force, Position, and Stiffness for Robot Joints Powered via Pneumatic Muscles

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***Abstract*—This paper proposes a novel controller framework for antagonistically driven pneumatic artificial muscle (PAM) actuators. The proposed controller can be stably configured in both torque-stiffness control and position-stiffness control modes. Three contributions are sequentially presented in constructing the framework: i) A PAM force feedback controller with guaranteed stability is synthesized in a way so as to contend with nonlinear PAM characteristics. ii) A mathematical tool is developed to compute reference PAM forces, for a given set of desired joint torque and joint stiffness inputs. iii) On top of the torque controller, a position control scheme is implemented and its stability analysis is given in the sense of Lyapunov. In order to test the controller framework, an extensive set of experiments were conducted using an actuator that was constructed using two antagonistically coupled PAMs. As the result, the actuator exhibited satisfactory tracking performances concerning both torque-stiffness control and position-stiffness control modes.**

***Index Terms*—pneumatic artificial muscle, compliant actuator, force and position control, variable stiffness.**

## I. Introduction

INCORPORATION of passive compliance in modern day actuators leads the way to the advancement of human friendly robotics, a design and control concept in which humans and robots safely co-exist and co-operate [1]–[3]. Contrary to the predominant robotics design approach which makes use of non-backdrivable and stiff actuators, this concept exploits the passivity properties of compliant actuators in a way so as to address stability, inherent safety, low output impedance, energy efficiency, and enhanced adaptability [1], [4]–[7]. Biological structures exploit this feature by means of adaptive control [8], [9], to create mechanically favorable energetics, and to stabilize unstable dynamics during environmental interactions [10], [11].

In the light of these shreds of evidence, a wide range of variable stiffness actuators has been developed for robotic applications [7], [12]. Within this context, PAMs (Pneumatic Artificial Muscle) could exhibit advanced characteristics over electrical actuators [13], [14]. They possess superior power-to-weight ratios and have no requirement for heavy frictional gears [7]. Furthermore, the physical compliance property enables the incorporation of inherent safety and adaptivity; they can potentially emulate their biological counterparts in this sense. While the constant need of pressurized air appears to be an inevitable drawback, PAMs were successfully employed in various robotic systems [15]–[21].

To name a few successful implementations, Zhao et al. exploited the physical compliance of PAMs for enhanced legged locomotion control [16]. Further implementations used the compliance property for advanced physical interactions in exoskeleton control [17], [18]. The researchers made use of pneumatic actuation to achieve active tactile sensing for soft morphological control in [19]. Ohta et al. developed a 7-DoF (Degrees of Freedom) robot arm actuated via PAMs to ensure safe and dependable human-robot interaction [20]. For a more comprehensive review, one can refer [21]. Therefore, it is evident that the PAMs have a wide range of applications in robotics due to their numerous favorable properties.

A pair of antagonistically coupled muscles could enable the simultaneous control of torque and stiffness [8], [9]. Despite the fact that PAMs can exhibit the variable stiffness behavior, this feature may not be sufficiently exploited in PAM-actuated robotics. In one of a few examples, Tondu and Lopez demonstrated that PAMs can be used as a torque and stiffness generator while using Hogan's model [22]. Bicchi and Tonietti utilized variable stiffness of PAMs while considering minimum-time optimal control with safety constraints [21]. Sardellitti et al. proposed a method to adjust stiffness by means of a sliding mode controller, applied to an average PAM-valve model [23].

Sharing the common ground with [8], this paper proposes a novel controller for an actuator that is powered via an antagonistically coupled PAM pair. The proposed controller can be stably configured in both simultaneous torque-stiffness control and simultaneous position-stiffness control modes. Despite several impressive studies, earlier reports may not fully address simultaneous control of force, position and variable stiffness in terms of feedback control with proven stability conditions.

Within this context, this paper chiefly contributes towards this direction with the following qualities: i) the synthesis of a stable PAM force feedback controller with proven passivity, so as to cope with nonlinear PAM characteristics, ii) a comprehensive mathematical model to interpret joint torque and variable torsional stiffness inputs in terms of individual muscle

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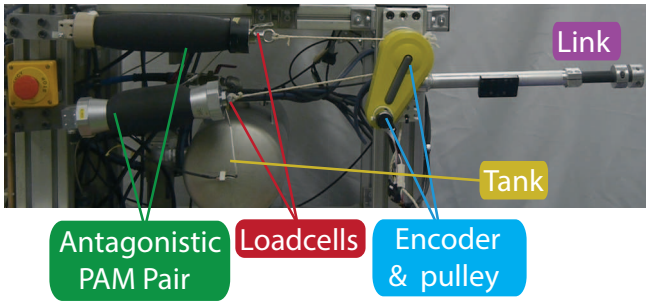


Fig. 1. The experimental test bench. Pressure servo valves are placed separately, and therefore, not displayed. Agonist muscle PAM-a is the one at the top; see Fig. 2.

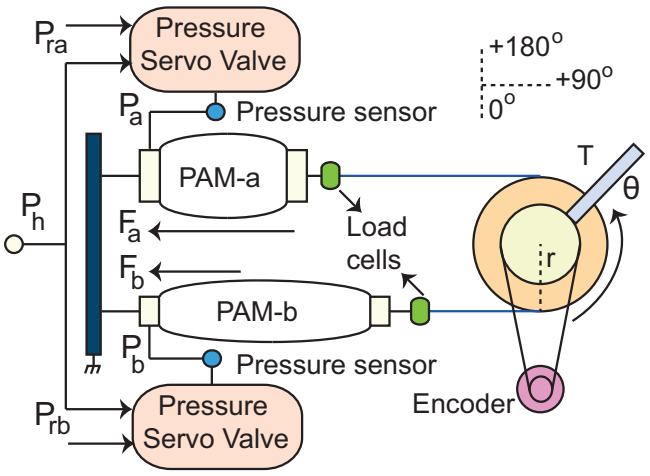


Fig. 2. Main elements of the experimental test bench. PAM-a is the agonist muscle while PAM-b is the antagonist muscle.

forces for achieving simultaneous torque & stiffness control mode, iii) a position & stiffness control mode with guaranteed stability including multi-DoF dynamics, iv) an extensive set of experiment tests concerning both control modes.

The paper is organized as follows: The hardware setup used in our experiments and our PAM modeling approach are succinctly introduced in Section II. Stable control modes (torque-stiffness control and position-stiffness control) are disclosed in Section III, together with their stability analyses. Experimental results are presented in Section IV. The paper is concluded in Section V, with discussions on the results.

## II. Experimental Test Bench and PAM Modeling

One of the main objectives in our research is the development of *soft* exoskeletons with adjustable stiffness property, as they possess several advantages in terms of human-robot co-existence. To this end, a 1-DoF actuator module was developed to serve as an experimental test bench to evaluate the real-time performance of controllers; see Fig. 1.

The module was powered via a pair of antagonistically coupled PAMs (Festo MAS-40), including servo pressure valves (NORGREN, VP5010SBJ series, 0-8 bar) to control inner pressure in proportion to the applied voltage inputs. PAMs were mechanically attached using a pulley-cable system. Cable lengths are adjusted while considering maximum PAM contraction and desired motion range: 60 to 110 degrees; see Fig. 2. An encoder is deployed at the pulley to measure the actual joint angle, and therefore, PAM length variations. The valves can also output actual pressure measurements.

The maximum torque output is limited with $\pm 60$ Nm, by considering the maximum allowable force for the cable. Each PAM length is 22 cm when the input pressure is 0 bar; this drops to 15.5 cm when fully contracted. Custom-made hardware was used for control electronics. The sampling rate was kept at 250 Hz. In Fig. 2, $F_a$ and $F_b$ are PAM forces, measured via load cells (FUTEK, LCM300-FSH03755). $P_a, P_b$ are measured pressure values, $P_{ra}, P_{rb}$ are referential pressure values, $T$ is the output torque produced by the actuator, $r$ is the pulley radius, $\theta$ is the joint angle and $P_h$ is the supply pressure. A significantly rigid link is attached to the output of the actuator.

For PAM-powered actuators, one may construct a model to characterize the pressure-force-length relation mathematically. For this purpose, we combined the modeling approaches reported in [24]–[26] as follows:

$$\begin{aligned} F(P,L,\dot{L}) &= P\sum_{\mathbf{u}=0}^{2}\mu_{\mathbf{u}}L^{\mathbf{u}} - \left(\sum_{\mathbf{j}=0}^{4}\eta_{\mathbf{j}}L^{\mathbf{j}} + \eta_5 L^{\frac{2}{3}}\right) \\ &- \operatorname{sgn}(\dot{L})\left(\lambda_2\dot{L}^2 + \lambda_1\dot{L} + \lambda_0(1-e^{-\frac{|\dot{L}|}{\lambda_3}})\right) \quad (1) \\ &= P\beta - \gamma \quad (2) \end{aligned}$$

In (1), $P$ and $L$ respectively denote PAM pressure and length, while $F$ represents the PAM force generated due to contraction. $\beta = \beta(L)$ and $\gamma = \gamma(L,\dot{L})$ are used to arrange equations in a clear way. In order to obtain the coefficients in (1), namely, $\mu_{\mathbf{u}}$ (**u**=0..2), $\eta_{\mathbf{j}}$ (**j**=0..5), $\lambda_{\mathbf{k}}$ (**k**=0..3), a parameter identification routine was executed with 160000 collected samples of force, pressure, length and length rate change. The coefficients may vary in the range of $\pm 10^6$. In this procedure, a chirp signal was assigned as the pressure input; its amplitude and frequency were varied between 0-8 bar and 0.1-4 Hz, respectively. Load cells, deployed at each PAM tip, are used to collect force data. Individual PAM lengths ($L_a$, $L_b$), are obtained using the actual joint angle,

$$L_a = L_{0a} - r(\theta - \theta_0), \qquad L_b = L_{0b} + r(\theta - \theta_0), \qquad (3)$$

where $\theta_0$ is the initial joint angle when both PAM pressures at their minimum. $L_{0a}$ and $L_{0b}$ are the PAM length values when $\theta = \theta_0$. In fact, the PAM model comprises the cable in series, since the encoder at the joint is used to measure length $L$. This automatically allows us to incorporate cable stiffness in the model. A parameter identification procedure was performed via a nonlinear least square fitting method. As the result, the maximum modeling error percentage stayed within the band of $\pm 2.5\%$ For details concerning data collection, modeling, and tuning, refer to [27] and [28].

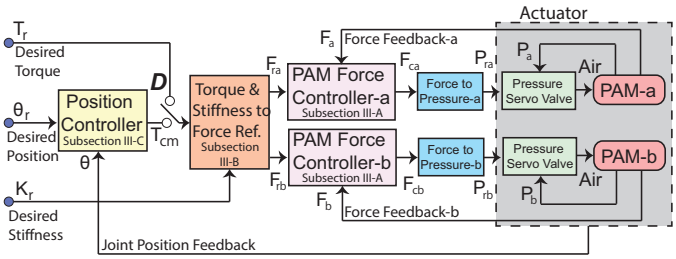


Fig. 3. The control framework, it is constituted as a cascaded architecture. The key $D$ allows the choice between two control modes: i) simultaneous torque-stiffness control, or ii) simultaneous position-stiffness control.

## III. Control Framework

The controller framework is depicted in Fig. 3. In this figure, $\theta_r$, $\theta$, $T_r$, $T_{cm}$ and $K_r$ indicate desired joint angle, actual joint angle, desired joint torque, command torque (position controller output) and desired joint stiffness, respectively. $F_{ri}$, $F_i$, $F_{ci}$, $P_{ri}$, and $P_i$ sequentially denote desired force, actual force, command force (force controller output), reference pressure, and actual pressure for the $i^{th}$ PAM; $i$=$a, b$. Underscripts $a$ and $b$ respectively associate PAM parameters with agonist and antagonist muscle units.

The cascaded controller framework in Fig. 3 is sequentially constructed as follows.

A) To track desired force inputs, each PAM is controlled through a force feedback controller with guaranteed stability; see subsection III-A.

B) Using this architecture, we develop a mathematical tool which computes desired PAM forces ($F_{ra}$, $F_{rb}$) for a given set of desired joint torque input ($T_r$ in torque control mode or $T_{cm}$ in position control mode) and joint stiffness input ($K_r$); see subsection III-B.

C) On top of the torque controller, a position control scheme is implemented; see subsection III-C. In this case, variable stiffness control option is still viable, since the output of the position controller is linked to the torque input port.

The switch $D$ in Fig. 3 allows the choice between two control modes: i) simultaneous torque-stiffness control, ii) simultaneous position-stiffness control.

### A. Stable Force Feedback for a Single Muscle

The $i^{th}$ PAM force feedback controller with guaranteed stability is illustrated in Fig. 4 [27]. Reference pressure inputs are inserted to proportional servo valves, as they ensure reliable pressure tracking control. Although we have no information regarding the servo valve inner control structure, we may use a linear first order model to describe the mathematical relation between the reference pressure and actual pressure [23], [27].

$$\epsilon \dot{P}_i = -P_i + P_{ri} \tag{4}$$

In (4), $\epsilon$ is the time constant which can be experimentally characterized. $P_{ri}$ is computed by inserting the $i^{th}$ force command $F_{ci}$ to the related force-pressure model; see Fig. 3. Force-pressure model was given in (2). With this in mind, the combination of (2) and (4) yields the following.

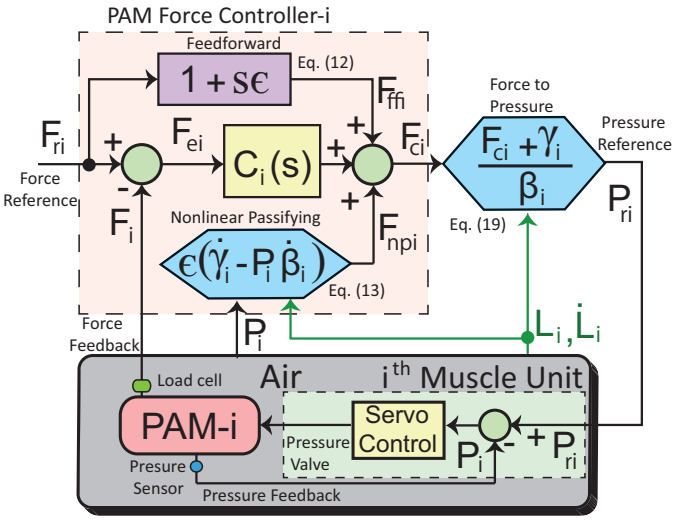


Fig. 4. Force feedback controller for a single PAM unit. The light pink block (PAM Force Controller-i) shows the details of the controller. See Fig. 3 for the role of this controller within the overall framework. The pressure valve, indicated with a light green block with dashed frame, includes a built-in servo controller and is responsible for pressure tracking. It also provides pressure measurements: $P_i$. Blue heptagon blocks indicate function blocks. In the feedforward block, $s$ is the Laplace variable to indicate time differentiation. Measurements of $L_i$ and $\dot{L}_i$ are readily available via an encoder deployed in the joint unit; see Figs. 1 and 2.

$$\dot{P}_i = -\frac{P_i}{\epsilon} + \frac{F_{ci} + \gamma_i}{\epsilon \beta_i} \tag{5}$$

Subtracting the actual force from the desired force outputs the force error, $F_{ei}$.

$$F_{ei} = F_{ri} - F_i = F_{ri} - (P_i \beta_i - \gamma_i) \tag{6}$$

Despite the mapping $F_{ci} \mapsto F_{ei}$ is not passive, it is possible to render plant (eqs. (5)-(6)) passive with respect to the mapping $\upsilon_i \mapsto F_{ei}$, in which $\upsilon_i$ is an external input to be defined. In this case, the storage function, $S(P)$, is assigned as follows.

$$S(P) = \frac{1}{2} \epsilon F_{ei}^2 \tag{7}$$

The first derivative of (7) is as follows.

$$\begin{aligned} \dot{S}(P) &= \epsilon F_{ei} \dot{F}_{ei} = \epsilon F_{ei} (\dot{F}_{ri} - \dot{F}_i) \\ &= \epsilon F_{ei} (\dot{F}_{ri} - \dot{P}_i \beta_i - P_i \dot{\beta}_i + \dot{\gamma}_i) \end{aligned} \tag{8}$$

Plugging (5) into (8),

$$\dot{S}(P) = F_{ei} (\epsilon (\dot{F}_{ri} - P_i \dot{\beta}_i + \dot{\gamma}_i) + P_i \beta_i - \gamma_i - F_{ci})), \tag{9}$$

and recalling that $F_i = P_i \beta_i - \gamma_i$,

$$\dot{S}(P) = F_{ei} (\epsilon (\dot{F}_{ri} - P_i \dot{\beta}_i + \dot{\gamma}_i) + F_i - F_{ci}). \tag{10}$$

Command force (force controller output) $F_{ci}$ is designated as follows.

$$F_{ci} = F_{ri} + \epsilon(\dot{F}_{ri} - P_i\dot{\beta}_i + \dot{\gamma}_i) - \upsilon_i. \quad (11)$$

In force command (11), $\upsilon_i$ is the external control input. $\epsilon(\dot{\gamma}_i - P_i\dot{\beta}_i)$ stands for nonlinear passifying terms, whereas $F_{ri} + \epsilon\dot{F}_{ri}$ indicate the feedforward input. They can be explicitly expressed as below.

$$F_{ffi} = F_{ri} + \epsilon\dot{F}_{ri} \quad (12)$$

$$F_{npi} = \epsilon(\dot{\gamma}_i - P_i\dot{\beta}_i) = \epsilon\left(\frac{\partial\gamma_i}{\partial L_i}\dot{L}_i - P_i\frac{\partial\beta_i}{\partial L_i}\dot{L}_i\right) \quad (13)$$

In (13), we utilized the chain rule to obtain $\dot{\gamma}_i$ and $\dot{\beta}_i$, since the rate change of PAM length $\dot{L}_i$ is readily available. Partial differentiations can be formulated with the help of eqs. (1) and (2):

$$\frac{\partial\gamma_i}{\partial L_i} = 4\eta_4 L_i^3 + 3\eta_3 L_i^2 + 2\eta_2 L_i + \eta_1 + \frac{2}{3}\eta_5 L_i^{-\frac{1}{3}} \quad (14)$$

$$\frac{\partial\beta_i}{\partial L_i} = 2\mu_2 L_i + \mu_1 \quad (15)$$

Placing (11) in (10), $\dot{S}(P)$ reduces to the following.

$$\dot{S}(P) = F_{ei}(F_i - F_{ri} + \upsilon_i) = F_{ei}(-F_{ei} + \upsilon_i) \quad (16)$$

$$= -F_{ei}^2 + F_{ei}\upsilon_i \leq F_{ei}\upsilon_i \quad (17)$$

Equation (17) reveals that the plant (5)-(6), along with the $F_{ci}$ command that includes nonlinear passifying and feedforward terms, is a strictly passive system with respect to input $\upsilon_i$ and output $F_{ei}$ [29]. Control input $\upsilon_i$ is constructed using a lead-lag controller; see $C_i(s)$ in Fig. 4.

$$\upsilon_i = -F_{ei}C_i; \quad C_i(s) = K_{xi}\Xi_i\frac{1 + T_{Ii}s}{1 + \Xi_i T_{Ii}s}\frac{1 + T_{Di}s}{1 + \alpha_i T_{Di}s} \quad (18)$$

In (18), we have $0 \leq T_{Di} < T_{Ii}$, $1 \leq \Xi_i < \infty$, and $0 \leq \alpha_i < 1$ [29]; $K_{xi}$, $T_{Di}$, $T_{Ii}$, $\Xi_i$, $\alpha_i$ are the controller gains that were tuned empirically according to standard rules of linear controller design; stability and non-excitation of unmodeled nonlinear dynamics. Their values are given in Table I for each PAM. Note that controller gains slightly differ for each PAM, since they have minor differences, e.g., length.

Finally, the force command $F_{ci}$ can be converted to pressure commands for the servo valves by using (2) in a reverse order.

$$P_{ri} = \frac{F_{ci} + \gamma_i}{\beta_i} \quad (19)$$

One may wonder whether the passifying control command $F_{ci}$ in (11) has actually provided a dynamic linearization via feedback. Indeed, by making use of (5), (6) and (11), the closed-loop systems reads as follows.

$$\epsilon\dot{F}_{ei} = -F_{ei} + \upsilon_i \quad (20)$$

It is then straightforward to design a linear controller to stabilize (20) to the origin $F_{ei} = 0$. Incorporating the nonlinear passifying terms and feedforward terms with the feedback control action ($F_{ei}C_i$) via (11) is the consequence of the stability analysis. In this case, the plant with the pre-compensator (combination of nonlinear passifying and feedforward terms) and the controller establish a system with passive feedback interconnections. Referring to the direct implication given in (17) for this case, the system is asymptotically stable and Bounded-Input-Bounded-Output stable [29].

Synthesizing the controller using this theory not only proves the stability but also reveals a controller with high tracking performance thanks to nonlinear passifying and feedforward terms. The controller compensates certain nonlinearities that are intrinsic to PAM actuators, enabling our feedback controller to exhibit favorable tracking performance. In practice, the sole implementation of the classical feedback controllers (PID or lead-lag only, without feedforward and nonlinear passifying terms) revealed unacceptable tracking performance and frequently led to instability.

TABLE I
LEAD-LAG COMPENSATOR VALUES FOR EACH PAM UNIT.

| | $K_{xi}$ | $T_{Di}$ | $T_{Ii}$ | $\Xi_i$ | $\alpha_i$ |
|---|---|---|---|---|---|
| PAM-a | 2.1 | 0.21 | 0.42 | 1.08 | 0.56 |
| PAM-b | 2.3 | 0.23 | 0.45 | 1.06 | 0.59 |

### *B. Torque and Variable Stiffness Control Mode*

To achieve torque and stiffness control, we develop a mathematical tool that converts desired joint torque and variable stiffness ($T_r$, $K_r$) to reference PAM force inputs ($F_{ra}$, $F_{rb}$), for both agonist and antagonist muscles. In connection with Fig. 2, $T_r$ may be obtained in terms of $F_{ra}$ and $F_{rb}$ as below.

$$T_r = r\left(F_{ra} - F_{rb}\right) \quad (21)$$

Desired joint stiffness, $K_r$, can be derived using a partial differentiation of (21) with respect to joint angle $\theta$ [8]. This approach may not characterize the effect of air flow; therefore, a certain amount modeling uncertainty is present.

$$K_r = \frac{\partial T_r}{\partial\theta} = r\left(\frac{\partial F_{ra}}{\partial L_a}\frac{\partial L_a}{\partial\theta} - \frac{\partial F_{rb}}{\partial L_b}\frac{\partial L_b}{\partial\theta}\right) \quad (22)$$

$$= r^2\left(\frac{\partial F_{ra}}{\partial L_a} + \frac{\partial F_{rb}}{\partial L_b}\right) \quad (23)$$

To yield (23), the chain rule is applied to (22) with eq. (3) [23]. Evaluating (23), we need to differentiate force equations (eq. (1)) with respect to PAM lengths for the $i^{th}$ muscle unit.

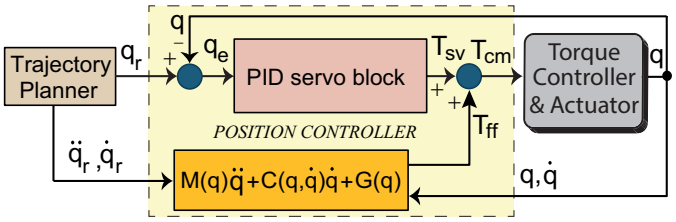


Fig. 5. Computed torque control with PID is chosen as the position controller. The light yellow block corresponds to the Position Control block in Fig. 3. For clarity, the rest of the blocks concerning the torque & stiffness to PAM forces, individual PAM force controllers and the actuator are summed up within the gray block, named 'Torque Controller & Actuator'.

$$
\begin{aligned}
F_{ri} &= P_{ri}\sum_{\mathbf{u}=0}^{2}\mu_{\mathbf{u}i}L_i^{\mathbf{u}} - \sum_{\mathbf{j}=0}^{4}\eta_{\mathbf{j}i}L_i^{\mathbf{j}} - \eta_{5i}L_i^{\frac{2}{3}} \\
&- \operatorname{sgn}(\dot{L}_i)\left(\sum_{\mathbf{k}=0}^{2}\lambda_{\mathbf{k}i}\dot{L}_i^{\mathbf{k}} + \lambda_{3i}e^{-\frac{|\dot{L}_i|}{\lambda_{4i}}}\right) \qquad (24)\\
&= P_{ri}\beta_i - \gamma_i \qquad (25)\\
\frac{\partial F_{ri}}{\partial L_i} &= P_{ri}\sum_{\mathbf{u}=1}^{2}\mathbf{u}\mu_{\mathbf{u}i}L_i^{\mathbf{u}-1} + \frac{\partial P_{ri}}{\partial L_i}\beta_i \\
&- \sum_{\mathbf{j}=1}^{4}\mathbf{j}\eta_{\mathbf{j}i}L_i^{\mathbf{j}-1} - \frac{2}{3}\eta_{5i}L_i^{-\frac{1}{3}} \qquad (26)\\
&= P_{ri}\Phi_i + \frac{\partial P_{ri}}{\partial L_i}\beta_i - \Psi_i \qquad (27)
\end{aligned}
$$

In (24) and (26), $\mu_{\mathbf{u}i}$ ($\mathbf{u}$=0..2), $\eta_{\mathbf{j}i}$ ($\mathbf{j}$=0..5), and $\lambda_{\mathbf{k}i}$ ($\mathbf{k}$=0..4) are PAM model parameters and identified for both muscles. The functions $\beta_i$, $\gamma_i$, $\Phi_i$ and $\Psi_i$ are used to clarify the notation. In addition, $\frac{\partial P_{ri}}{\partial L_i}$ term is insignificant when the actuator volume is much smaller than the air tank volume [15], [23]. Therefore, $\frac{\partial P_{ri}}{\partial L_i}\beta_i$ term is practically negligible. In [27], an attempt for this formulation included a misconception; yet, the corresponding error was observed to be insignificant.

$$
K_r = r^2\left(\frac{\Phi_a}{\beta_a}(F_{ra}+\gamma_a) + \frac{\Phi_b}{\beta_b}(F_{rb}+\gamma_b) - \Psi_b - \Psi_a\right) \qquad (28)
$$

Equations (21) and (28) constitute a set of formulae to compute joint torque and stiffness, in terms of PAM forces. Since our main purpose is to obtain PAM forces in terms of joint torque and stiffness, (21) and (28) are solved to obtain PAM forces. As such, the following computation is performed.

$$
\begin{aligned}
F_{ra} &= \frac{\beta_a\beta_b}{\Phi_a\beta_b + \Phi_b\beta_a}\left(\frac{K_r}{r^2} + \Psi_b + \Psi_a - \frac{\Phi_a}{\beta_a}\gamma_a\right. \\
&- \left.\frac{\Phi_b}{\beta_b}\left(\gamma_b - \frac{T_r}{r}\right)\right) \qquad (29)\\
F_{rb} &= F_{ra} - \frac{T_r}{r} \qquad (30)
\end{aligned}
$$

### C. Position and Variable Stiffness Control Mode

The torque controller described in subsection III-B enables us to construct a reliable position control scheme on top of it. To attain this goal, we make use of the Computed Torque Control [30] whose block diagram is displayed in Fig. 5. In this figure, the trajectory planner is responsible for the generation of reference joint angles ($q_r$), depending on the task-specific robot motion. The controller makes use of the robot dynamics; therefore, the position control performance can be enhanced.

Although the hardware setup we use in our experiments is 1-DoF, we present a stability proof for a multi-DoF system to show the generality of the controller. Thus, we use the *so-called* reduced flexible multi-DoF robot dynamics [31].

$$
\begin{aligned}
M(q)\ddot{q} + C(q,\dot{q})\dot{q} + G(q) &= T + T_{ext} \qquad (31)\\
T_{cm} &= T - Kq - B_p\dot{q} - J_p\ddot{q} \qquad (32)
\end{aligned}
$$

In (31) and (32), $M(q)$, and $G(q)$, and $C(q,\dot{q})$ are inertial, gravity, and coriolis & centrifugal terms, respectively. $T$ is the output torque, $q$ is the joint angle vector, $T_{cm}$ is the task-specific command torque (the output of the position controller in this case), $T_{ext}$ is the external disturbance torque. $K$, $B_p$ and $J_p$ are diagonal matrices that represent joint stiffness, pulley friction and pulley inertia. Since there are no gear nor mechanical transmission, $B_p$ is negligibly small. $J_p$ is also very small and omitted. Keeping this in mind, the combination of (31) and (32) yields the following.

$$
M(q)\ddot{q} + C(q,\dot{q})\dot{q} + G(q) - Kq - T_{cm} - T_{ext} = 0 \qquad (33)
$$

Utilizing the following computed torque control, $T_{cm}$ is defined as below:

$$
\begin{aligned}
T_{cm} &= G(q) + M(q)\ddot{q}_r \\
&+ K_p q_e + K_v\dot{q}_e + K_i\int_0^t q_e\,dt + C(q,\dot{q})\dot{q}_r. \qquad (34)
\end{aligned}
$$

The joint angle error is $q_e$ which is obtained via $q_e = q_r - q$. $K_p$ and $K_i$ and $K_v$ are diagonal matrices that store positive PID gains. Plugging (34) into (33) results as follows:

$$
M(q)\ddot{q}_e + (C(q,\dot{q}) + K_v)\dot{q}_e + (K_p - K)q_e = \tilde{\nu}, \qquad (35)
$$

where $\tilde{\nu} := \nu + d$, $d := -Kq_r - T_{ext}$, and $\nu := -K_i\int_0^t q_e\,dt$.

We are now going to prove that, for any basin of attraction $\Omega_l := \left\{(q_e,\dot{q}_e,\tilde{\nu}) \in \mathbb{R}^{3n} : \|(q_e,\dot{q}_e,\tilde{\nu})\| \le l\right\}$ $q_r(t), T_{ext}(t)$, we can always select PID gains $K_p, K_i, K_v$ such that, for any constant $d(t), t \ge 0$ and for any initial condition in $\Omega_l$, the error dynamics converges to zero, i.e. $(q_e(t),\dot{q}_e(t)) \to 0$ as $t \to +\infty$.

To this end, we propose a Lyapunov function candidate as follows [32],

$$
\begin{aligned}
V &= \frac{1}{2}\dot{q}_e^\top M(q)\dot{q}_e + \frac{1}{2}q_e^\top\left(K_p - K - \frac{1}{\varepsilon}K_i\right)q_e + \varepsilon q_e M(q)\dot{q}_e \\
&+ \frac{\varepsilon}{2}\left(-\frac{1}{\varepsilon}K_i q_e + \tilde{\nu}\right)^\top K_i^{-1}\left(-\frac{1}{\varepsilon}K_i q_e + \tilde{\nu}\right), \qquad (36)
\end{aligned}
$$

which is positive definite and radially unbounded on $\Omega_l$ when $\varepsilon$ is sufficiently small. Furthermore, $K_p$ and $K_i$ gains are properly tuned so as to ensure $\varepsilon(K_p - K) - K_i$ is positive definite.

By taking the time derivative of $V$ along the solutions of (35), we have:

$$\dot{V} = -\begin{pmatrix}\dot{q}_e\\ q_e\end{pmatrix}^\top \underbrace{\begin{pmatrix}K_v - \varepsilon M & \frac{\varepsilon}{2}(K_v - C^\top)\\ \frac{\varepsilon}{2}(K_v - C) & \varepsilon(K_p - K) - K_i\end{pmatrix}}_{A(q,\dot{q})} \begin{pmatrix}\dot{q}_e\\ q_e\end{pmatrix}, \tag{37}$$

where we made use of the skew symmetry property $\dot{M} - 2C$.

The $A(q, \dot{q})$ is positive definite on $\Omega_v$ when the following Schur complement conditions are met,

$$\varepsilon(K_p - K) - K_i \succ N \succ 0, \tag{38}$$

$$K_v \succ \varepsilon m_2 I + \frac{\varepsilon^2}{4}\left(K_v - C^\top\right) N^{-1} \left(K_v - C^\top\right), \tag{39}$$

where $N$ is an arbitrary positive definite matrix. Furthermore, $m_1 I < M < m_2 I$ in which $m_1$ and $m_2$ are non-negative scalar numbers and $I$ is an identity matrix with proper dimension; $|C(q, \dot{q})| < k_c|\dot{q}_e| < k_l$ where $k_c$ and $k_l$ are nonnegative scalar numbers. PID gains are empirically tuned in accordance with the above convergence analysis such that (36), (38) and (39) and hold true. Therefore, by a direct application of LaSalle's principle, we conclude that $q_e(t), \dot{q}_e(t) \to 0$ as $t \to +\infty$. For our case, these gains are assigned as $K_p = 166.67$, $K_i = 2.83$, and $K_v = 4.17$.

## IV. Experiment Results

All the experiments were conducted on the 1-DoF test bench; see section II. Due to safety precautions, input characteristics were kept within certain limits in a way that force references do not exceed 1600 N. Refer to the multimedia attachment to view certain scenes from the experiments.

### A. Force Control

As explained previously, simultaneous position/torque and variable stiffness control problems were converted to individual PAM force control. Therefore, it is of importance to ensure reliable force tracking for each muscle. To this end, we conducted force control experiments on a single PAM unit and compared its performance with respect to the conventional method in which a PID+Feedforward controller was utilized [22]. The gains of the conventional controller were empirically tuned, i.e., they were set for the maximum possible performance without causing unstable oscillations. The results are plotted in Fig. 6, Fig. 7, and Fig. 8.

In Fig. 6, a step input with an amplitude of 700 N was implemented as the force reference and it is indicated via blue dash-dotted line. The response of the proposed and conventional controllers are respectively plotted via solid green and purple lines. As may be observed, the proposed controller exhibited a good performance; it converged to the reference with a settling time of 0.5 s, and 5% overshoot. The steady-state error was measured to be approximately 5 N. For the case of conventional controller, the steady-state error was approximately 110 N. It also converged to a constant value after 1.9 s.

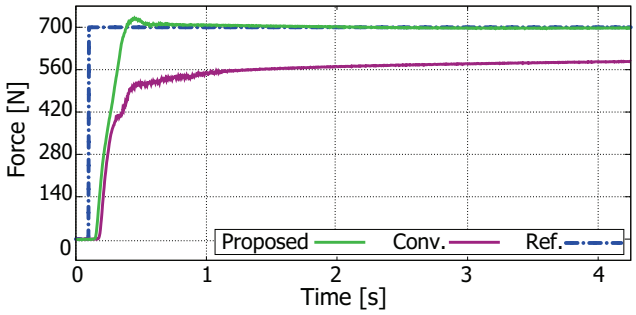


Fig. 6. Force control results for a step input with an amplitude of 700 N.

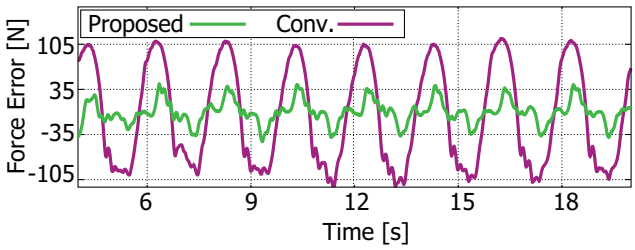


Fig. 7. Force tracking error graphics for a sine wave input at 0.5 Hz.

In Fig. 7 and Fig. 8 sine input signals were implemented. The frequency of sine wave was 0.5 Hz in Fig. 7 and 2.0 Hz in Fig. 8. Force tracking error signals were depicted via solid green and purple lines for the proposed and conventional controllers, respectively. For the case of conventional controller, the force error stayed within $\pm 105$ N and $\pm 150$ N bands for 0.5 Hz and 2.0 Hz input signals, respectively. On the contrary, the proposed controller exhibited more favorable results, and reduced the force tracking error for about 67% in each case.

The proposed force controller can take PAM nonlinearities into account, and therefore, outperformed the conventional controller. Therefore, it provided a solid basis to establish simultaneous position/torque and variable stiffness control. As the proposed controller includes a feedback linearization loop (nonlinear passifying terms), it had a larger control bandwidth. In contrast, we had a relatively more limited bandwidth in the case of conventional controller as it does not comprise nonlinear terms.

### B. Simultaneous Torque and Stiffness Control

Simultaneous torque and variable stiffness tracking control experiment results are presented in Figs. 9(a)-(b) and Figs. 10(a)-(b), in which dotted blue, solid cyan, dotted red and solid green lines respectively indicate reference and response torque and stiffness variations.

In Fig. 9(a), torque reference input was a sine wave signal with a frequency of 2.0 Hz and with a peak-to-peak amplitude of 30 ($\pm$15) Nm. In Fig. 9(b), stiffness reference input was a sine wave with a frequency of 0.5 Hz and a peak-to-peak amplitude of 30 (60$\pm$15) Nm/rad. In this experiment, torque input frequency was chosen different than the stiffness input frequency; 2.0 Hz $>$ 0.5 Hz. Despite the difference in input

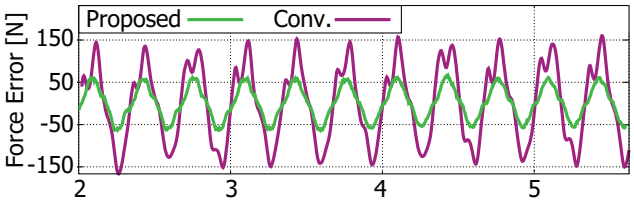


Fig. 8. Force tracking error graphics for a sine wave input at 2.0 Hz.

frequencies, the controller showed a satisfactory performance, concerning both joint torque and joint stiffness tracking.

Fig. 10(a) and Fig. 10(b) depict simultaneous torque and stiffness tracking results from a similar experiment. In contrast to the previous experiment, torque and stiffness reference input frequencies were assigned as 0.5 Hz and 2.0 Hz, respectively; 0.5 Hz $<$ 2.0 Hz. Amplitudes were kept the same as in the previous experiment. Similar to the previous case, the controller exhibited favorable tracking performances regarding the simultaneous joint torque and stiffness control.

Force tracking performances of each PAM are displayed in Fig. 9(c) and Fig. 10(c). Agonist muscle (PAM-a) reference and measured forces are represented via dotted blue and solid cyan lines. Antagonist muscle (PAM-b) reference and actual forces are indicated with dotted red and solid green lines. Scrutinizing Fig. 9(c), one can observe that the PAM force references appear to be the interference pattern of two input frequencies, namely, torque input (2.0 Hz) and stiffness input (0.5 Hz). A similar case with different interference pattern may be observed in Fig. 10(c) as well. In both cases, force references were tracked well, thanks to the stabilized force control strategy. It is the force feedback controller (see Fig. 4) that ensures the simultaneous torque and stiffness control, simply by tracking the individual PAM force references.

### C. Position Control Experiments: Constant Stiffness

In order to solely display position control with constant stiffness, we conducted joint tracking experiments with a 2.5 kg dumbbell, which is attached to the actuator tip as the payload.

Fig. 11 displays position tracking performances when the stiffness reference is set to a constant value. One can assign this value freely within the physical limits. In our experiments, it was 65 Nm/rad. In this figure, dotted blue and solid cyan lines respectively stand for reference and measured joint position variations. Actual joint angles were measured via the encoder. In Fig. 11(a), the input signal was a sine wave at 0.5 Hz with a peak-to-peak amplitude of 40° (65°∼105°). In Fig. 11(b), the input frequency was 2.5 Hz and had a peak-to-peak amplitude of 10° (85°∼95°). The amplitude was deliberately kept low for 2.5 Hz input to ensure safety during the experiment. Fig. 11 indicates that the position tracking was satisfactory and assured for both low and high-frequency reference inputs.

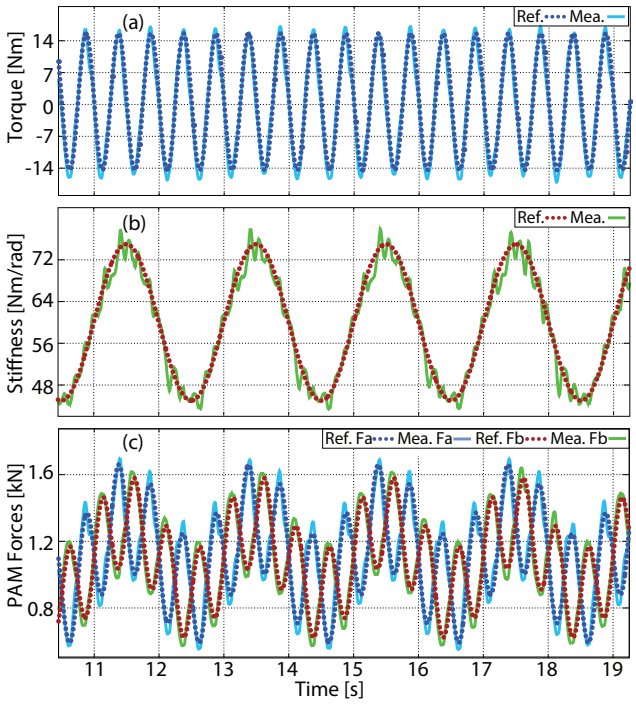


Fig. 9. a) Torque tracking results for a sine wave input at 2.0 Hz. b) Stiffness tracking results for a sine wave input at 0.5 Hz. c) Individual PAM force tracking results. $F_a$ and $F_b$ stand for agonist and antagonist muscle forces, respectively; see Fig. 2. Torque input signal frequency was greater than stiffness input signal frequency; 2.0 Hz $>$ 0.5 Hz.

### D. Simultaneous Position and Stiffness Control

In Fig. 12(a)-(b) and Fig. 13(a)-(b), simultaneous position and stiffness tracking plots are displayed, where dotted blue, solid cyan, dotted purple and solid green lines respectively point out reference joint position, actual joint position, reference joint stiffness and response joint stiffness. In Figs.12(c) and 13(c), force tracking performances can be examined for each PAM unit. Agonist muscle (PAM-a) reference and measured forces are represented via dotted blue and solid cyan lines. Antagonist muscle (PAM-b) reference and actual forces are indicated with dotted red and solid green lines.

For the results included in Figs. 12(a)-(b), position and stiffness inputs were generated via $5^{th}$ order polynomials. The position reference trajectory starts from 80° when $t = 5.3$, and arrives at 100° when $t = 6.5$. Stiffness reference trajectory starts from 45 Nm/rad when $t = 5.0$, and arrives at 75 Nm/rad when $t = 7.5$. As a result, we obtained satisfactory position and variable stiffness tracking performances, despite a minor fluctuation in stiffness tracking. Once the trajectories were ended, both stiffness and position values settled to their terminal references. In this particular experiment, the stiffness trajectory period was deliberately chosen longer than the position trajectory; however, an inverse pattern can also be successfully realized in our system without any restriction.

In Figs. 13(a)-(b), position and stiffness inputs were generated via sine waves. Position and stiffness reference input frequencies were 1.5 Hz and 0.8 Hz, respectively. Peak-to-peak amplitudes of these inputs were 20° (80°∼100°), and

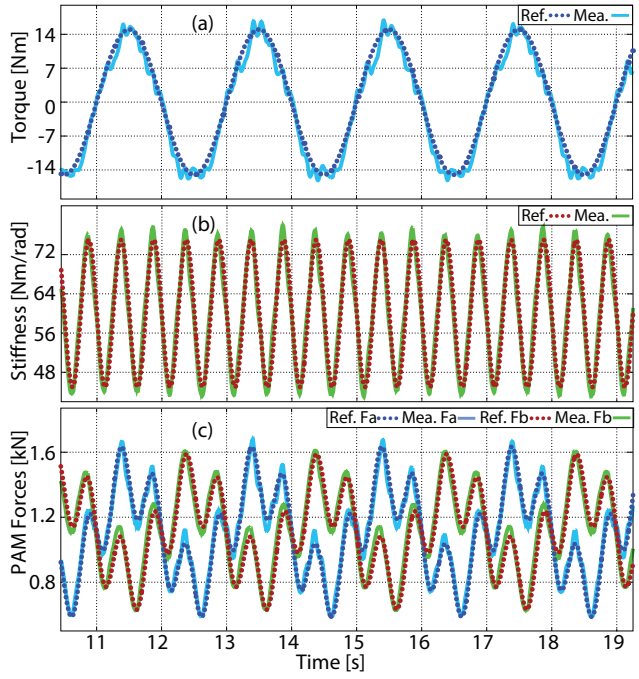


Fig. 10. a) Torque tracking results for a sine wave input at 0.5 Hz. b) Stiffness tracking results for a sine wave input at 2.0 Hz. c) Individual PAM force tracking results. $F_a$ and $F_b$ stand for agonist and antagonist muscle forces, respectively; see Fig. 2. Stiffness input signal frequency was greater than torque input signal frequency 2.0 Hz $>$ 0.5 Hz.

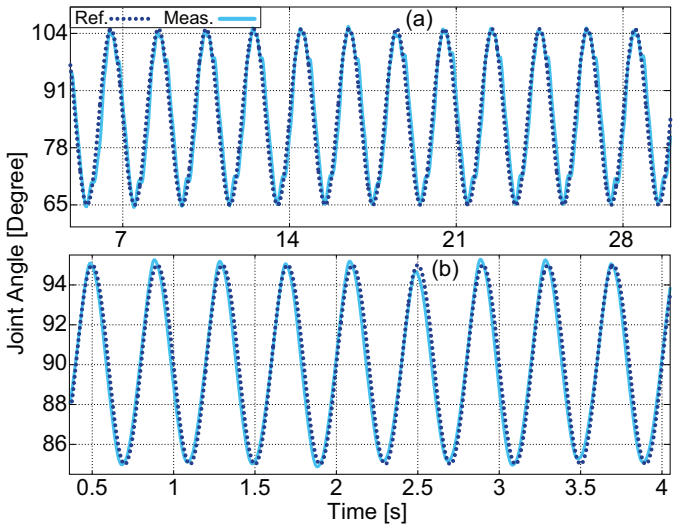


Fig. 11. Position tracking when the stiffness was set to 65 Nm/rad. a) Sine wave with an input frequency of 0.5 Hz. c) Sine wave with an input frequency of 2.5 Hz.

20 Nm/rad (50 Nm/rad$\sim$70 Nm/rad). Observing this figure, we can see that the controller provided favorable position and variable stiffness tracking performances, despite the fact that input frequencies were chosen differently.

The output of the position controller is the torque command; see Fig. 5. Therefore, individual PAM reference forces are the interference pattern of the command torque and stiffness inputs. With this in mind, we added force tracking results for each muscle unit in Fig. 12(c) and Fig. 13(c). Similarly,

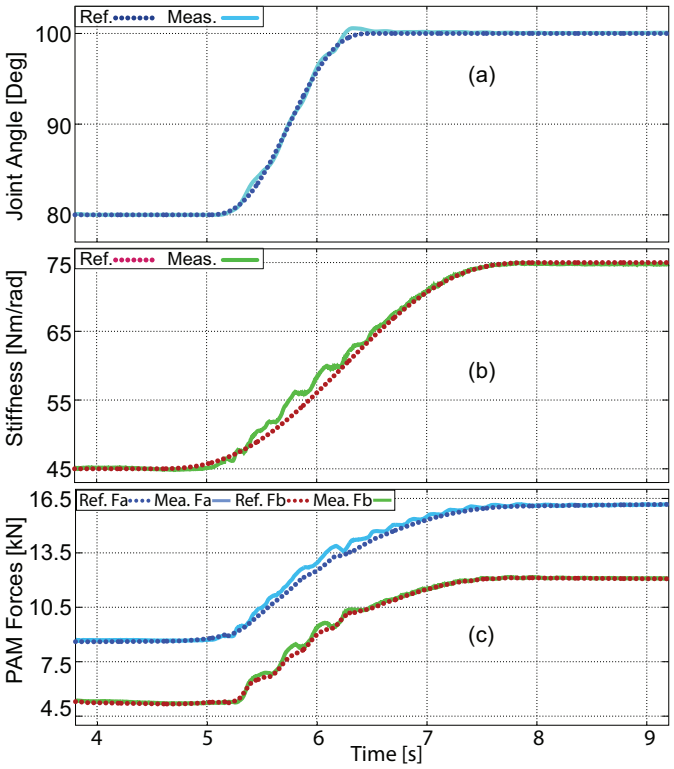


Fig. 12. Position and stiffness tracking results for inputs generated via $5^{th}$ order polynomials. a) Position reference trajectory starts from 80° when $t = 5.3$, and arrives at 100° when $t = 6.5$. b) Stiffness reference trajectory starts from 45 Nm/rad when $t = 5.0$, and arrives at 75 Nm/rad when $t = 7.5$. c) Force profile and tracking of each muscle to execute this motion.

agonist muscle (PAM-a) reference and measured forces are represented via dotted blue and solid cyan lines. Antagonist muscle (PAM-b) reference and actual forces are indicated with dotted red and solid green lines. These results show that the individual PAM force tracking was assured as well, both for polynomial and sinusoidal position and stiffness inputs.

## V. Conclusion

In this paper, we proposed a novel controller framework for actuators, powered via antagonistically driven pneumatic artificial muscles. The controller can be configured in two stable control modes: a) simultaneous torque and variable stiffness control, b) simultaneous position and variable stiffness control. Using a detailed model that encapsulates intrinsic PAM nonlinearities (friction, nonlinear elasticity), and synthesizing effective control techniques that account for those nonlinearities, the actuator exhibited favorable tracking performances in both control modes. An extensive set of hardware experiments validated the controller, as the actuator exhibited favorable tracking performances when configured in both control modes.

In constructing this controller, three main contributions are offered: i) A PAM force feedback controller with guaranteed stability was synthesized using the dissipativity theory. The controller was able to cope with the inherent nonlinearities of PAMs, which occur due to frictional and nonlinear elasticity terms. ii) Based on a detailed PAM model, a set of equations were derived to compute PAM references which correspond

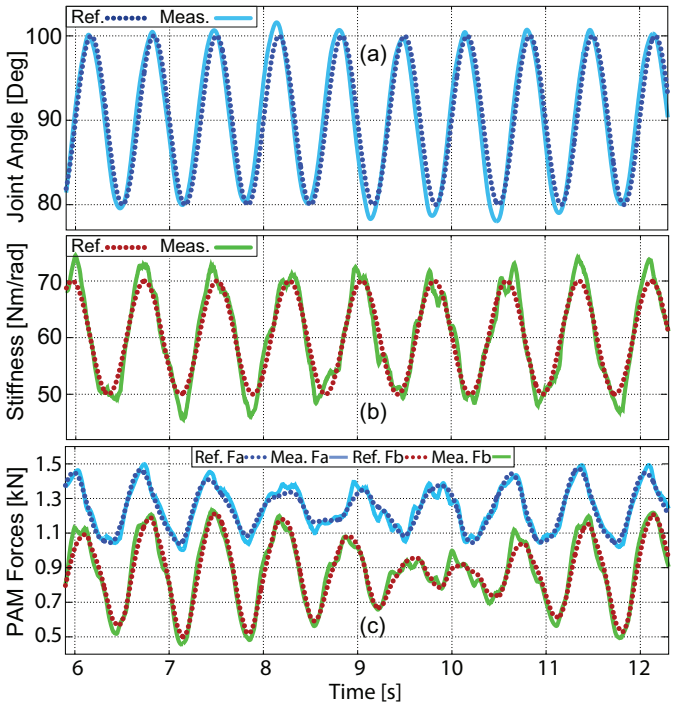


Fig. 13. Position and stiffness tracking results for inputs generated sine waves. a) Position reference input at 1.5 Hz with a peak-to-peak amplitude of 20°. b) Stiffness reference input at 0.8 Hz with a peak-to-peak amplitude of 20 Nm/rad. c) Force profile and tracking of each muscle to execute this motion.

to desired joint torque and stiffness inputs. Together with the stable PAM force feedback controller, this strategy allowed us to associate feedback control for the simultaneous torque-stiffness control task. iii) As we obtained a reliable torque controller, a position controller that is compatible for multi-DoF robots was derived and its stability conditions were demonstrated via Lyapunov's theory.

Since PAMs can generate only unidirectional forces, it is a strict obligation to use antagonistic setups to create bidirectional joint torque. Therefore, there is an actuator redundancy for this type of actuators. We believe that controlling the variable stiffness is a very efficient way of exploiting this redundancy, as PAMs have nonlinear elasticity characteristics. Simultaneous torque and stiffness control is also observed in biological structures as well; they tune the muscle impedance characteristics by means of adaptive control to maintain stable postures and optimize mechanical energetics [9]–[11]. Considering this fact, PAM-powered actuators with variable stiffness control option can emulate biological muscles in this manner.

One particular aspect in overall controller performance is that stiffness control may be slightly out of track during dynamic transitioning. This may be due to the fact that stiffness controller does not have direct sensory feedback. Unlike stiffness, torque and position can be directly measured and fedback via load cells and encoders. However, stiffness tracking solely relies on model-based stiffness-force transmission and inner force control loops. One possible way to remedy this issue may be the utilization of stiffness sensors [33]. In order to further improve the tracking controllers, one may increase the sampling frequency and use sensors with higher resolution so that PAM force controller performance can be enhanced.

When performing simultaneous control, it is observed that the low frequency input has high frequency harmonics which may arise due to unmodeled coupling effects. Although the amplitude of these harmonics are well contained, one can eliminate these harmonics by using more comprehensive modeling approaches. Therefore, this issue is addressed as a future work.

Already, our research group implemented the proposed controllers to our multi-DoF exoskeleton systems, powered via PAMs, so as to address robot-aided rehabilitation, power augmentation and active walking assist studies in rehabilitation centers [17]. Our next work will focus on the exploitation of adjustable stiffness feature for robot-aided neuro-rehabilitation applications in terms of inherently safe, synergistic, and stable human-robot interaction.

## ACKNOWLEDGEMENTS

This research was supported by the Commissioned Research of NICT, ImPACT of CSTI, NEDO, JST-Mirai Program No.JPMJMI18B8 Japan, and JSPS KAKENHI No.JP16H06565.

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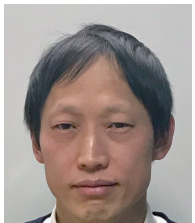

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